

EVALUATION ON THE COURSE "TWO-PHASE FLOWS WITH PHASE CHANGE"

WEDNESDAY FEBRUARY 1ST, 2023

Vertical evaporator for cooling electronic devices

Refrigerant R134a at a pressure of 10 Bars enters a tube of 4mm diameter at a temperature of 30°C and a pressure of 10 bars. The tube is heated by the thermal dissipation of electronic component with a constant heat flux of 1W/cm².

The mass flux G is equal to 200 kg/m²/s.

The physical properties of R134a at saturation temperature $T_{sat}=39.4^\circ\text{C}$ at 10 bars are:

- densities of liquid and vapour : $\rho_l=1147.6 \text{ kg/m}^3$, $\rho_v=48.8 \text{ kg/m}^3$
- dynamic viscosities of liquid and vapour : $\mu_l=1.64 \cdot 10^{-4} \text{ Pa}\cdot\text{s}$, $\mu_v=12.5 \cdot 10^{-6} \text{ Pa}\cdot\text{s}$,
- latent heat of vaporisation $h_{LV}=163230 \text{ J/kg}$,
- heat capacity at constant pressure for liquid $C_{pl}=1497 \text{ J/kg/K}$,
- surface tension $\sigma=6.1 \cdot 10^{-3} \text{ N/m}$,
- thermal conductivity for liquid $\lambda=0.074 \text{ W/m/K}$,
- Prandtl number $Pr=3.28$.

1°/ The flow enters in single-phase liquid regime at $T_{le}=30^\circ\text{C}$ in the evaporator. Calculate the evolution of the liquid temperature $T_L(z)$ and the wall temperature $T_p(z)$ as a function of the vertical position z ($z=0$ at the entrance) by using Dittus-Boelter correlation for the heat transfer coefficient in single-phase flow H_l :

$$Nu = \frac{H_l D}{\lambda} = 0,023 \left(\frac{GD}{\mu_l} \right)^{0,8} Pr^{1/3}$$

2°/ Calculate the value of $z=z_{sat}$ at which the mean liquid temperature will be equal to the saturation temperature $T_L(z_{sat})=T_{sat}$. Justify that for $z=z_{sat}$, the onset of nucleate boiling is reached by using Frost and Dzakowic correlation :

$$T_p - T_{sat} > \left[\frac{8\sigma T_{sat} q}{\lambda Q_v h_{lv}} \right]^{1/2} \frac{1}{Pr}$$

3°/ For $z > z_{sat}$, express the quality x versus z . Calculate the values of the superficial velocities of liquid j_L and gas j_v for $z=0.3 \text{ m}$, $z=0.6 \text{ m}$. By using the flow pattern map (Figure 1) determine the flow pattern at the different locations. At which z value, the flow becomes pure vapor.

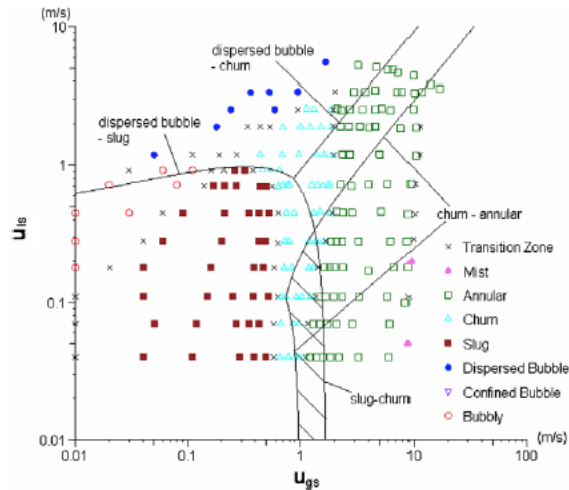


Figure 1 : Flow pattern map for R134a at 10bar in a 4 mm diameter tube according to Chen and Karayannis (2006)

4°/ At $z=0.3\text{m}$ and $z=0.6\text{ m}$, determine the wall temperature using Gunger et Winterton correlation :

$$H = H_1 \left[1 + 3000 \left(\frac{q}{Gh_{lv}} \right)^{0.86} + \left(\frac{x}{1-x} \right)^{3/4} \left(\frac{\rho_l}{\rho_v} \right)^{0.41} \right] \text{ with } H_1 = \frac{\lambda}{D} 0.023 \left(\frac{G(1-x)D}{\mu_l} \right)^{0.8} Pr^{1/3}$$

Plot the evolution of the wall temperature and the liquid temperature. Comment the result.

5°/ Evaluate the void fraction at $z=0.3\text{m}$ and $z=0.6\text{m}$ using relevant drift flux models, that will be justified:

$$U_v = \frac{j_v}{R_v} = C_0(j_v + j_L) + U_\infty$$

6°/ Using the momentum balance equation for the mixture, evaluate the pressure difference between $z=0$ and $z=0.6\text{m}$. Explain the physical meaning of the different terms.

$$\frac{d}{dz} \left[\frac{G^2 x^2}{\rho_v R_v} + \frac{G^2 (1-x)^2}{\rho_l R_l} \right] = -\frac{dp}{dz} + \frac{\tau_p 4}{D} - (\rho_l R_l + \rho_v R_v)g$$

The terms will be first calculated for $z < z_{sat}$ in single-phase flow. For $z > z_{sat}$, the hydrostatic pressure gradient will be evaluated using an average value of the void fraction between $z=0.3\text{m}$ and $z=0.6\text{m}$. The frictional pressure gradient will be calculated either at $z=0.3\text{m}$ or $z=0.6\text{m}$, using Lockhart and Martinelli model.